

## REMARKS

This housekeeping amendment is a duplicate of the Amendment filed in response to the aforementioned non-final Office Action (hereafter "Office Action") in relation to the Reissue Application for U.S. Patent No. 5,848,159 (hereafter the "original patent"). All changes presented herein have been made vis-à-vis the original patent to be issued.

### I. Reexamination Proceedings and Reissue Application Merged

Merger of the Reexamination proceedings 90/005,733 and 90/005,776, with respect to the original patent and the Reissue Application 09/694,416 (for the reissue of the original patent) is hereby acknowledged (See: Section 1 in the Detailed Action of the Office Action). In keeping with the procedures set forth for handling the merged proceedings, and to maintain prosecution and examination consistency between the Reissue and Reexamination proceedings, Applicants will submit a separate Housekeeping Amendment in each of the Reexamination proceedings.

### II. Status of the Claims

As of the date of this Amendment, claim 8 of the original patent is canceled, claims 1-7 and 9-13 of the original patent are amended and remain pending; new claims 14-61 were added in the preliminary amendment and, of these claims, claims 14-40, 42, 43, 45-47, 50-56 and 58-61 are hereby amended. Thus, claims 1-7 and 9-61 are now pending in the Reissue Application.

### III. Claim Designated for Printing in the Official Gazette

Claim 1 is designated for printing in the Official Gazette upon allowance of this Reissue Application.

### IV. Statement of Support for the Amendments in the Disclosure of the Original Patent

#### **A. All changes made vis-à-vis the original patent**

All the amendments presented herein, including amendments to the written description and the claims, have been made vis-à-vis the original patent. Accordingly, the amendments presented herein include the amendments previously presented in the Preliminary Amendment,

which was filed concurrently with this Reissue Application, to the extent that such amendments are to be maintained. Moreover, the statements of support for the amendments herein, even if some have already been stated before in the Preliminary Amendment and repeated herein, are provided in their entirety for completeness and clarity.

## **B. The Specification**

The specification of the original patent has been amended to correct typographical errors and other matters of form and to render the specification consistent throughout and with the claims. Support for the amendments to the specification may be found throughout the original patent. No new matter has been introduced by the amendments to the specification.

In general, changes embodying corrections of typographical errors and other matters of form are self-explanatory and need no further explanation. As to the mathematical expressions, equations expressing any congruence of the form  $b=c(\text{mod } m)$  or the like, where  $b$  is congruent to  $c$  and  $m$  is the modulus, are mathematically written in proper form as  $b \equiv c(\text{mod } m)$ . Accordingly all the equations are written in proper form, e.g.,  $C \equiv M^e(\text{mod } n)$ . Where applicable, the parentheses (e.g., around "mod  $n$ ") are properly added as well.

Support for amendments to the paragraph beginning at column (hereafter "col."), line 4 may be found in col. 1 of the cover page. Support for the amendments to the paragraph beginning at col. 3, line 23 and the paragraph beginning at col. 3, line 27 may be found for example at col. 2 of the cover page and col. 13, lines 44-47.

Support for amendments to the paragraph beginning at col. 3, line 36, may be found at column 5, lines 31-33. Support for amendments to the paragraph beginning at col. 3, line 56, may be found for example at col. 3, lines 20-26, col. 3, lines 44-55 and col. 4, lines 9-11. Support for amendments to the paragraph beginning at col. 4, line 6, may be found for example at col. 3, lines 20-26, col. 4, lines 6-12, 32-34 and 52-56.

Support for amendments to the paragraph beginning at col. 4, line 13 and the paragraph beginning at col. 4, line 50, may be found for example at col. 3 line 42, col. 4, line 41, and col. 10, lines 54-56. Further support for amendments to the paragraph beginning at col. 4, line 50 may be found at col. 4, lines 50-52.

Support for paragraph inserted before the paragraph beginning at col. 5, line 52, may be found for example at col. 14, lines 30-36 and 45-49. Support for amendments to the paragraph beginning at col. 5, line 30, may be found for example at col. 2, lines 5-10, col. 3, line 42, col. 4 line 41, col. 5, line 39, col. 10, line 65 and col. 11, lines 8-9. Further support for amendments to the paragraph beginning at col. 5, line 30, may be found in the multitude of mathematical expressions where  $d$ , the private key portion, is the "exponent," e.g.,  $M \equiv C^d \pmod{n}$  at col. 6, lines 1-5.

Support for amendments to the paragraph beginning at col. 6, line 24, may be found for example at col. 5, lines 31-33, col. 6, line 37 (" $M=Y_k...$ "), col. 7, line 15, and col. 11, lines 15-20. Support for amendments to the paragraph beginning at col. 6, line 65, may be found for example at col. 6, lines 1-4, 26-35, 40-53 and 67. Support for amendments to the paragraph beginning at col. 7, line 1, may be found for example at col. 2, lines 32-34 and 40, col. 3, lines 22-26, col. 4, lines 32-34, col. 6 line 38 and col. 7, lines 56-58.

Support for amendments to the paragraph beginning at col. 8, line 1, is found in col. 8 line 3 (i.e., FIPS 140-1 with level 3 is a well known standard, See: <http://csrc.nist.gov/fips/fips1401.htm>). Support for amendments to the paragraph beginning at col. 10, line 15, may be found for example at Figure 3. Support for amendments to the paragraph beginning at col. 10, line 35, may be found for example in col. 10 line 40 and line 53 (i.e.,  $M$  is represented by a numerical value greater than 0 and smaller than  $n$ ).

### C. The Claims

Claims 1-7 and 9-13 of the original patent have been amended to correct typographical errors and other matters of form, to explicitly recite subject matter which is implicitly included in the claimed invention, and/or to more clearly and particularly recite the subject matter which Applicants regard as their invention. New claims 14-61 have been added to further point out and distinctly claim the subject matter that Applicants regard as their invention.

For the Examiner's convenience, a clean version of the amended claims (as now presented) is provided herewith as Exhibit A. As stated above, the amendments herein are made vis-à-vis the original patent (notwithstanding the prior changes to the claims in the Preliminary Amendment). But to show the difference between the claims presented in the Preliminary

Amendment and the claims presented herein a mark-up version showing the changes relative to the Preliminary Amendment is provided as **Exhibit B**.

Support for the amendments to claims 1-7 and 9-13 and for the added claims, 14-61, may be found throughout the original patent. No new matter has been introduced by this amendment.

In general, claim amendments embodying corrections of typographical errors, antecedent basis errors, and other matters of form are self-explanatory and need no further explanation. As to the mathematical expressions, equations expressing any congruence of the form  $b = c(\text{mod } m)$  or the like, where  $b$  is congruent to  $c$  and  $m$  is the modulus, are mathematically written in proper form as  $b \equiv c(\text{mod } m)$ . Accordingly all the equations are written in proper form, e.g.,  $C \equiv M^e(\text{mod } n)$ . Where applicable, parentheses (e.g., around "mod  $n$ ") are properly added as well.

Also, by and large, claim amendments representing a change to the preamble of the original and new (added) independent claims find support throughout Applicants' original patent. Particularly, support for the recitation of *communications of a message cryptographically processed with RSA (Rivest, Shamir & Adleman) public key encryption*, is implicitly present in the mathematical expressions throughout Applicants' original patent. Additionally, support for this recitation is explicitly present in the summary at col. 3 and col. 4, in the detailed description at col. 5 et seq. as well as in the Rivest patent (4,405,829) which is incorporated by reference into the original patent (See, e.g., col. 1, lines 56-63). Accordingly, this particular amendment will not be addressed again with respect to each individual claim.

Support for the amendments to claim 1 as now presented may be found, for example, at claims 1, 5 & 6 as presented in the original patent as well as at col. 1, lines 32-42 & 43-54, col. 3, lines 7-12, 22-25 & 39-44, col. 4, lines 6-8 & 32-48, col. 5, lines 30-36, 40-46 & 58-63, and col. 10, lines 25-34. Support for the amendments to claim 2 as now presented may be found, for example, at the original claims 2 & 4 as well as at col. 5, lines 36-50. Similarly, support for amendments to claims 3-7 and 9-13 as now presented may be found, for example, at claims 1-7 and 9-13 as presented in the original patent. Further support for the amendments to claims 3-7 and 9-13 as now presented may be found for example at col. 1, lines 32-42 & 43-54, col. 3, lines 39-44, col. 5, lines 30-50, col. 7, line 44 to col. 10, line 44. Further support for amendments to claims 9-13 as now presented may be found for example at col. 9, lines 16-23 & 47-58.

As to the newly added claims, support for claim 14-23 and 40-59 may be found, for example, at col. 1, lines 32-45, col. 3, lines 30-50, col. 4, lines 32-49, col. 5, lines 30-51, col. 5,

line 66 to col. 6, line 25, col. 7, line 44 to col. 10, lines 44. Further support for new claims 14-23 and 40-59 may be found at claims 1-13 as presented in the original patent. For example, support for new claims 18 and 19 may be found in claim 9, i.e., col. 14, lines 30-36. Also, support for new claims 24-39 may be found for example at column 3, lines 36-65, col. 4, lines 8-12, 32-38 & 50-56 and col. 5, lines 58-63. Support for new claims 42-52 may be found at Figures 1-3, and the accompanying description at col. 7, line 34 to col. 10, lines 44. Further support for new claims 50-54 may be found at col. 5, line 52 to col. 6, line 6. Finally, support for claims 60 and 61 may be found at col. 4, lines 6-13 and col. 5, lines 61-63.

#### **V. Supplemental Reissue Oath and Declaration**

Applicants appreciate the reminder about a Supplemental Reissue Oath and Declaration (See: Section 3 in the Detailed Action of the Office Action, or simply Section 3 of the Office Action). Applicants will submit that Oath and Declaration document at the close of prosecution, after allowance of this Reissue Application.

#### **VI. Consent by Assignee, Certificate Establishing Rights of Assignee, and Assignments**

In reference to Sections 4 & 5 of the Office Action, where it is stated that the Reissue Application is objected to as lacking written consent of all assignees, including Tandem Computers Inc. ("Tandem") and Compaq Computer Corp. ("Compaq"), Applicants point out that the requirements under 37 CFR §§1.172 & 3.73 have been met. For the Examiner's convenience Exhibit C includes a copy of documents which show compliance with these requirements, including: Consent of Assignee to this Reissue Application, Certificate under 37 CFR 3.73(b), Notice of Recordation of the Assignment from the inventors to Tandem and Notice of Recordation of Merger Documents relating to the merger of Tandem into Compaq. A copy of the stamped return postcard showing filing the said documents is also provided.

To recap, the inventors (Collins et al.) assigned their invention (U.S. Application No. 08/784,453) to Tandem, which Assignment has been recorded on May 7, 1997 at Reel/Frame 8542/0875. In turn, Tandem assigned its Patent Applications and issued Patents to Compaq when Tandem merged into Compaq. To that end, the Merger Documents have been filed with the Assignment Division in relation to the aforementioned U.S. Patent 5,848,159 (which issued from the 08/784,453 Application to Collins et al. on December 8, 1998, and the reissue of which is

now being sought). As the enclosed Notice of Recordation of the Merger Documents indicates, the Merger Documents have been recorded on October 16, 2000 at Reel/Frame 011190/0457.

Accordingly, all the requirements under 37 CFR §§1.172 & 3.73 have been met. Respectfully, in view of the foregoing the objection to this Reissue Application should be reconsidered and withdrawn.

## **VII. The Drawings**

In reference to Section 6 of the Office Action, where it is stated that new formal drawings are required, Applicants hereby comply. Attached herewith are new formal drawings, including Figures 1-3.

## **VIII. Preliminary Amendment Entered**

In Section 7 of the Office Action it is indicated that the Preliminary Amendment, filed concurrently with this Reissue Application, has been entered. Applicants appreciate entry of the Preliminary Amendment and note that, notwithstanding, this amendment introduces changes vis-à-vis the original patent as required by 37 CFR §1.173(g).

## **IX. Three Information Disclosure Statements Considered**

In Section 8, the Examiner states that the information disclosure statements (IDSs) filed April 11, 2001 (4 references) and June 26, 2001 (2 references), respectively, were considered (on December 5, 2001 & June 4, 2002, respectively). On December 5, 2001, The Examiner considered also, but failed to mention, the IDS (13 references) filed concurrently with this Reissue Application. A copy of all three IDS was signed by the Examiner and returned with this Office Action. A copy of the three, signed IDSs is provided for the Examiner's convenience as **Exhibit D**.

## **X. Objection to the Specification**

### **A. New Matter**

Section 10 of the Office Action indicates that the [preliminary] amendment to the specification has been objected to under 35 U.S.C. §132 having allegedly introduced new matter to the specification. In particular, the objection to the added material at col. 5, line [62] relating to

'digital signatures' alleges that digital signatures have not been disclosed in the originally-filed specification (implicitly or explicitly).

However, the Examiner is kindly requested to note the recitations in claims 9 and 10 of the original patent. Likewise, it is implicit in RSA schemes, as disclosed in the original specification (e.g., col. 1, lines 55-62), that  $C \equiv M^d \pmod{n}$  [or  $M_s \equiv M^d \pmod{n}$ ] produces a value typically referred to as the "signature" (as the private key  $d$  is used in the encryption). Indeed, in col. 10, lines 35-37 & 42-44 it is suggested that a plaintext message can be encrypted/decrypted using the public/private key RSA scheme. Moreover, since the original patent incorporates by reference U.S. Patent 4,405,829 (See: Col. 1, line 61), the Examiner is kindly requested to also note, in the '829 patent, col. 3, line 9 et seq. col. 5, lines 45-47, and col. 8 line 56-67.

Namely, the aforementioned amendment to Col. 5 relating to the signature merely expresses that which is implicit and/or imports that which is incorporated by reference. Accordingly, it is respectfully submitted that no new matter has been introduced by the aforementioned amendment to Col. 5 relating to the signature. A reconsideration and withdrawal of the new matter objection under 35 U.S.C. §132 is hereby solicited.

## B. Informalities

As indicated in Sections 11-13 of the Office Action, the specification is objected to because of the error in equation 4 in the paragraph starting at col. 2 line 19, and because of a misstatement of line number [52] at col. 8. Applicants appreciate the Examiner's thorough review of the original patent and Preliminary Amendment and have corrected these deficiencies. As now presented equation 4 correctly recites:

$$\underline{M \equiv C^d \pmod{n}} \quad (4),$$

and the line number of the paragraph at col. 8 is changed to 62. The specification is now believed to be correct, and reconsideration and withdrawal of the objection to the specification based on informalities is hereby respectfully solicited.

## XI. Claim Objections

In Sections 14-17, the Examiner points out deficiencies in amendments to claim 3 as presented in the preliminary amendment. Claim 3 has been amended in accordance with the

mark-up version of the claims as shown herein above and is now believed to be correct (See, e.g.,  $M_x \leq n_y - 1$ , and  $C_x \equiv M_x^{-1} \pmod{n_y}$ ). Accordingly, reconsideration and withdrawal of the claim objections is respectfully requested.

## **XII. Claim Rejections under 35 U.S.C. §101; Rejections Rendered Moot by Amendments**

Sections 18-21 of the Office Action indicate that claims 7, 8 and 13 are rejected under 35 U.S.C. §101 as lacking utility (See: Sections 18-21 of the Office Action). Although the comments immediately below address these claim rejections, as later explained, the rejections have nonetheless been rendered moot by the claim amendments as presented herein above.

With reference to these rejections, the Examiner asserts that an invention that is useful for encryption only fails to provide utility and is of no use if it cannot be decrypted. Applicants respectfully disagree with the Examiner's characterization of the claimed invention (as recited in the earlier claim 7) and in view of that disagree that the claimed invention lacks utility. Indeed, as previously presented claim 7 did not provide only for encoding and did not preclude decoding (and claim 8 (now cancelled) explicitly recited a decoding key  $D_i$  for each terminal).

The Examiner also notes that the invention is directed, in general, to increasing the efficiency of an RSA cryptographic system and method. And, it is true that increasing the speed of encryption (by reducing the number of computation cycles) is useful, as the Examiner points out. Moreover, claim 7 as previously presented recited a method for 'establishing cryptographic communications' and encryption establishes cryptographic communications. Namely, the invention as recited in the earlier claim 7 produced the specifically useful result claimed by Applicants. Hence, earlier claims 7 and 8 did not lack utility.

Notwithstanding the foregoing, the claim rejections have been rendered moot by the claim amendments herein above. As will be later discussed in more detail, the claims have been amended (as shown herein above) to explicitly claim "communications of messages cryptographically processed with RSA public key encryption" (as is well known, RSA stands for Rivest, Shamir and Adleman). To be sure, a message can contain, for example, a DES key (data encryption standard key). Then, in accordance with this invention each messages, even if containing a DES key, is cryptographically processed using the RSA scheme.



It is respectfully submitted that all the claims produce the results claimed by Applicants and hence have utility. Accordingly, the claim rejections under 35 U.S.C. §101 should be reconsidered and withdrawn.

### **XIII. Claim Rejections under 35 U.S.C. §112**

#### **A. Enablement, 35 U.S.C. 112, 1<sup>st</sup> paragraph**

Claims 8 and 13 are rejected under 35 U.S.C. 112, 1<sup>st</sup> paragraph, for lack of enablement. (See: Sections 23-25 of the Office Action). Claim 8 has been cancelled without prejudice or surrender of subject matter and will not be discussed here. Claim 13, however, remains pending and is enabled by Applicants' disclosure including the disclosure that Applicants incorporated by reference into the written description. Claim 13 is enabled, for example, by the description in the original patent at col. 1, lines 54-55 and col. 7, lines 25-33, and in the 4,405,829 patent at col. 13, lines 29-46. Accordingly, reconsideration and withdrawal of the claim rejection under 35 U.S.C. 112, 1<sup>st</sup> paragraph is hereby respectfully requested.

#### **B. Distinctly Claiming Applicants' Invention, 35 U.S.C. 112, 2<sup>nd</sup> paragraph**

In Sections 26-30 of the Office Action the Examiner indicates that claims 24-39 are rejected under 35 U.S.C. 112, 2<sup>nd</sup> paragraph. However, the claim amendments obviate these claim rejections as the terms "faster than..." and "compatible with..." are not recited and the term "fewer computation cycles..." for multi-prime RSA is recited comparatively to the cycles for two-prime RSA. Applicants believe that given the above-outlined amendments to claims 24-39 Applicants' invention is particularly pointed out and distinctly claimed. Moreover, as mentioned in Section IV.C above, support for these claims is found in Applicants' disclosure. Accordingly, reconsideration of the claim rejections under 35 U.S.C. 112, 2<sup>nd</sup> paragraph is hereby respectfully requested.

### **XIV. THE INVENTION**

Before getting to the claim rejections in the next section (XV) an explanation of the invention is worthwhile. It is important that the invention be properly understood particularly in view of the assertions and analysis in the Office Action.

First, even though it is clear from the mathematical expressions throughout Applicants' disclosure, including the claims, that the invention involves RSA public key encryption, the claims have been amended to expressly point this out. As now presented, the claims make it expressly clear that they involve messages that are cryptographically processed with RSA public key encryption. Having said that, important aspects of the claimed invention are further explored.

Note for example claim 1. The clean version of claim 1 as now presented reads as follows:

1. (Twice Amended) A method for communications of a message cryptographically processed with RSA (Rivest, Shamir & Adleman) public key encryption, comprising the steps of:  
 developing  $k$  distinct random prime numbers  $p_1, p_2, \dots, p_k$ , where  $k$  is an integer greater than 2;  
 providing a number  $e$  relatively prime to  $(p_1 - 1) \cdot (p_2 - 1) \cdot \dots \cdot (p_k - 1)$ ;  
 providing a composite number  $n$  equaling the product  $p_1 \cdot p_2 \cdot \dots \cdot p_k$ ;  
 receiving a ciphertext word signal  $C$  which is formed by encoding a plaintext message word signal  $M$  to a ciphertext word signal  $C$ , where  $M$  corresponds to a number representative of the message and  $0 \leq M \leq n-1$ ,  
 where  $C$  is a number representative of an encoded form of the plaintext message word signal  $M$  such that  $C \equiv M^e \pmod{n}$ , and where  $e$  is associated with an intended recipient of the ciphertext word signal  $C$ ; and  
 deciphering the received ciphertext word signal  $C$  at the intended recipient having available to it the  $k$  distinct random prime numbers  $p_1, p_2, \dots, p_k$ .

In essence, claim 1 recites a method in which a message  $M$  is cryptographically processed (encoded) using the public key of a recipient  $(e, n)$ . The encoded message  $C \equiv M^e \pmod{n}$ , known as ciphertext, is received in that form without further modification by the recipient. That same (received) ciphertext  $C$ , is indeed decipherable by the recipient (using its private key  $(d, n)$ ). As is next explained, the recipient has available to it the  $k$  factors from which the modulus  $n$  is produced.

The recitation in claim 1 includes developing  $k$  distinct random prime numbers  $p_1, p_2, \dots, p_k$ , where  $k$  is an integer greater than 2 and further includes the fact that the modulus  $n$  is a composite number equaling the product  $p_1 \cdot p_2 \cdot \dots \cdot p_k$ . Namely, claim 1 recites that  $k > 2$  and the  $k$  prime numbers are random and distinct. Moreover, claim 1 recites that the modulus  $n$  is provided from a product of the  $k$  prime numbers. Contrast this (claim 1) recitation with selecting a modulus  $n$  and then factoring  $n$  to the  $k$  prime numbers.

It is important to understand and keep in mind that providing  $n$  as the product of  $p_1 p_2 \dots p_k$  having [already] available the  $k$  prime numbers makes it possible for them to be random and distinct. The randomness and distinctness attributes of the  $k$  prime numbers will materially improve the security in any cryptographic system with RSA public key encryption.

Moreover, the use of  $k > 2$  prime numbers allows improved efficiency of such system. As one would imagine, developing three or more prime numbers each of smaller size (relative to each of a pair of primes for the same size  $n$ ) takes fewer computation cycles than it would take for developing the pair of (larger) prime numbers. As an additional time-saving benefit, the  $k$  prime numbers allow parallel processing of encryption tasks.

By analogy, in each of the other claims (original and added claims)  $n$  is a product of the  $k$  prime factors, where  $k > 2$  and where the  $k$  prime factors are random and distinct. Again, contrast this with selecting a modulus  $n$  and then factoring  $n$  to  $k$  prime numbers (even if  $n$  were randomly selected). In addition, claims, including claims 2-6, 9, 11, 15, 16 etc., indicate that  $d$  (the private key portion) is established as a function of  $e$  (the public key portion) and the  $k$  prime numbers. As recited for example in claim 2,  $d$  is a multiplicative inverse of  $e(\text{mod}(\text{lcm}(p_1 - 1, p_2 - 1 \dots p_k - 1)))$ ; and, again, the  $k$  ( $k > 2$ ) distinct random prime numbers  $p_1, p_2, \dots p_k$  from which the modulus  $n$  is provided/computed are used for establishing  $d$ .

Within the scope and spirit of the invention as originally disclosed one would also recognize such variations as recited for example in claim 7. A clean version of claim 7 reads as follows:

7. (Amended) A method for communications of a message cryptographically processed with an RSA public key encryption, comprising the steps of:  
 developing  $k$  factors of a composite number  $n$ , the  $k$  factors being distinct random prime numbers and  $k$  is an integer larger than two ( $k > 2$ );  
 providing a number  $e$  relatively prime to a lowest common multiplier of the  $k$  factors;  
 providing the composite number  $n$ ;  
 receiving a ciphertext word signal  $C$  which is formed by encoding a digital message word signal  $M$  to the ciphertext word signal  $C$ , where said digital message word signal  $M$  corresponds to a number representative of said message and  
 $0 \leq M \leq n-1$ ,  
 where said ciphertext word signal  $C$  corresponds to a number representative of an encoded form of said message through a relationship of the form

$C \equiv a_e M^e + a_{e-1} M^{e-1} + \dots + a_0 \pmod{n}$   
 where  $e$  and  $a_e, a_{e-1}, \dots, a_0$  are numbers; and  
 deciphering the received ciphertext word signal  $C$  at an intended  
 recipient with knowledge of the  $k$  factors.

In essence, claim 7 has in common with claim 1 many of the important features that make this invention so advantageous, including the modulus  $n$  being a product of the  $k$  prime factors, where  $k \geq 2$  and where the  $k$  prime factors are random and distinct. In addition, as is the case in claim 1, the ciphertext message (here ciphertext word signal)  $C$ , which is formed by encoding the message (here digital message word signal)  $M$ , is received without further modifications. The variation from claim 1 has to do with the manner in which the ciphertext message  $C$  is formed. In claim 7, the ciphertext message  $C$  is formed as a function of  $M, n, e$  and coefficients  $a_e, a_{e-1}, \dots, a_0$ .

Yet another variation within the scope and spirit of the disclosed invention is provided in claim 9. A clean version of claim 9 reads as follows:

9. (Twice Amended) A system for communications of message signals cryptographically processed with RSA public key encryption, comprising:

$j$  terminals including first and second terminals, each of the  $j$  terminals being characterized by an encoding key  $E_i = (e_i, n_i)$  and decoding key  $D_i = (d_i, n_i)$ , where  $i=1, 2, \dots, j$ , each of the  $j$  terminals being adapted to transmit a particular one of the message signals where an  $i^{\text{th}}$  message signal  $M_i$  is transmitted from an  $i^{\text{th}}$  terminal, and

$0 \leq M_i \leq n_i - 1$ ,

$n_i$  being a composite number of the form

$n_i = p_{i,1} p_{i,2} \dots p_{i,k}$

where

$k$  is an integer greater than 2,

$p_{i,1}, p_{i,2}, \dots, p_{i,k}$  are distinct random prime numbers,

$e_i$  is relatively prime to

$\text{lcm}(p_{i,1}-1, p_{i,2}-1, \dots, p_{i,k}-1)$ , and

$d_i$  is selected from the group consisting of the class of numbers

equivalent

to a multiplicative inverse of

$e_i \pmod{\text{lcm}((p_{i,1}-1), (p_{i,2}-1), \dots, (p_{i,k}-1))}$ ;

said first terminal including

means for encoding a digital message word signal  $M_1$  to be transmitted from said first terminal ( $i=1$ ) to said second terminal ( $i=2$ ), said encoding means transforming said digital message word signal  $M_1$  to a signed message word signal  $M_{1s}$  using a relationship of the form

$M_{1s} \equiv M_1^{d_1} \pmod{n_1}$ ; and

means for transmitting said signed message word signal  $M_{1s}$  from said first terminal to said second terminal, wherein said second terminal includes  
 means for decoding said signed message word signal  $M_{1s}$  to said digital message word signal  $M_1$ .

As in the case of claim 7, claim 9 has in common with claim 1 important features of the invention, including the modulus  $n$  being a product of the  $k$  prime factors, where  $k \geq 2$  and where the  $k$  prime factors are random and distinct. Additionally in common with claim 1, the ciphertext message (here signed message word signal)  $M_{1s}$ , which is formed by encoding the plaintext message (here digital message word signal)  $M_1$ , is received without further modifications. The variation from claim 1 has to do with the manner in which the ciphertext message  $M_{1s}$  is formed. In claim 9, the encoded message  $M_{1s}$  is in fact a digital signature formed as a function of  $M_1$  and the private key of the sender ( $d, n$ ).

Although additional features and variations of the invention exist, the foregoing provides a constructive explanation of the invention. In view of this explanation, one would find it easier to understand why the claimed invention, as recited in claims 1-7 and 9-61, is novel and non-obvious. The patentable differences between the claimed invention and the cited references will be further addressed below with regards to the claim rejections.

## XV. Claim Rejections Under 35 U.S.C. §102

### A. Summary of Claim Rejections

In Sections 31-69 of the Office Action, where it is stated that the claims (1-61) are rejected under 35 U.S.C. §102, the Examiner cites, respectively, Rivest et al (U.S. Patent 4,405,829, hereafter "Rivest"), Vanston and Zuccheranto, "Using four-prime RSA in which some bits are Specified," Electronic Letters, Vol. 30, No. 35, 1994 (hereafter "Vanstone"), Captain Nemo, "RSA Moduli should have 3 Prime Factors," Scientific Bulgarian, August 1996, (hereafter "Nemo"), Slavin (U.S. Patent 5,974,151) and Itakura et al, "A Public-key Cryptosystem Suitable for Digital Multisignature," Nippon Electronic Co., Ltd., R&D No. 71, October 1983, IPSJ Journal Vol. 24, No. 4, May 2001 (hereafter "Itakura"). Rivest, Vanstone and Itakura have been relied on for rejecting the claims under 35 U.S.C. §102(b). Nemo and Slavin have been relied on for rejecting the claims under 35 U.S.C. §102(e).

**1. Nemo Cannot be Relied on for Rejection under 35 U.S.C. §102(e)**

Nemo is not a patent and therefore it cannot be relied on for rejecting the claims under 35 U.S.C. §102(e). As set forth in 35 U.S.C. §102(e), only a patent granted to another from an application filed prior to Applicants' date of invention can preempt allowance of this Reissue Application. Such is not the case with Nemo.

Since Nemo was published less than one (1) year prior to the filing date of the original patent (Dec. 9, 1996) it cannot be relied on for rejecting the claims under 35 U.S.C. §102(b) either. So, the only section remaining under which Nemo can be an alleged prior art is 35 U.S.C. §102(a).

**2. Nemo and Slavin are not necessarily prior art under 35 U.S.C. §102(a)**

Moreover, Nemo and Slavin may not qualify as prior art, regardless of what section of 35 U.S.C. §102 is used, including 35 U.S.C. §102(a). The alleged priority dates of Nemo and Slavin are August 1996 and November 1996, respectively, pre-dating the filing date of the original patent (Dec. 9, 1996) by only four (4) and one (1) months, respectively. Hence, Applicants reserve the right to contest the use of Nemo and Slavin as prior art reference, including by antedating their invention relative to these references.

**B. The Claimed Invention is Patentably Distinguishable from the Cited References: the Cited References do not Teach, Enable or Suggest the Claimed Invention**

It is well established that for anticipation to be established two requirements must be met: 1) the reference must teach each and every element of the invention; and 2) the reference must provide an enabling disclosure of the invention. Merely mentioning any aspect of the invention, without more, is insufficient to meet the anticipation requirements.

To recap, in keeping with the purpose of the claimed invention as set forth in claims 1-7 and 9-61, the modulus  $n$  is a product of the  $k$  prime factors, where  $k > 2$  and where the  $k$  prime factors are random and distinct. Furthermore, as set forth in the claims, e.g., claim 2,  $d$  (the private key portion) is established as a function of the  $k$  prime numbers and  $e$  (the public key portion). As recited for example in claim 2,  $d$  is a multiplicative inverse of  $e(\text{mod}(\text{lcm}(p_1 - 1, p_2 - 1 \dots p_k - 1)))$ ; and, again, the  $k$  ( $k > 2$ ) distinct random prime numbers  $p_1, p_2, \dots p_k$  from which the modulus  $n$  is provided/computed are also used for establishing  $d$ .

For clarity, it is perhaps better to first point out how this is different from the teachings of each of the cited references. These differences can then be related back to the claims.

Starting with **Rivest**, one of the references relied on by the Examiner, it is noted that Rivest is in fact incorporated by reference into the original patent. Rivest provides background information on the RSA public key encryption and sets the starting point for the claimed invention. No doubt, Rivest teaches and enables two-prime RSA public key encryption ( $n=p \cdot q$ ). However, although Rivest discloses that alternative embodiments may use  $n$  which is a product of three or more primes, it specifically also states (and teaching away from the present invention) that the primes need not be distinct (col. 13, lines 29-31). In further contrast to the claimed invention, Rivest also makes no mention of the fact that such primes are distinct and random. The mere mention of three or more prime numbers without more does not rise to the level of enabling disclosure that would allow someone to practice the claimed invention without undue experimentation. (Needless to say, no one in the RSA universe has produced a product embodying the multi-prime RSA technology until the original patent came to light.)

Although in col. 13, lines 29-34, Rivest mentions CRT (Chinese remainder theorem) and perhaps can be understood to suggest an approach using sub-tasks, Rivest does not mention performing such sub-tasks in parallel and indeed does not make a claim of improved performance as a result of using CRT (See: Section 50 of the Office Action). Moreover, Fig. 3, on which the Examiner relies (in Section 58), shows an encoding device (12) having registers (20, 22, 12, 24, 26 and 30), a multiplier selector (28) and a modulo  $n$  multiplier (32). As shown and described, neither the encoding device nor any part thereof are an exponentiation device. Namely, Rivest does not teach or suggest one or more exponentiation devices.

**Vanstone**, the next reference the Examiner relied on, is no more relevant than the foregoing reference. Vanstone introduces two concepts that address the need for added security with a stronger modulus. The first concept is using 4 prime factors in RSA which are selected from the same database as 2-prime RSA (See: Vanstone's *Introduction* and *Using four-primes RSA*). The second concept is selecting a set of primes that meet a non-random criteria. With these two concepts Vanstone teaches away from the present invention. Vanstone does not cover instances where the number of primes is  $K=3$  and  $K>4$ , and it merely teaches the extension of 2 prime factors to 4 prime factors for a greater modulus  $n$ . More importantly, Vanstone suggests using the same database of primes as was used in 2-prime RSA. Namely, randomly selecting a

number from an existing list or a database is not selecting a random number from the universe of prime numbers. What is more, the 4 prime factors of  $n$  are not random in that they are related in Vanstone through a relationship of the form  $p_i = 2^k f_i + a_k$  (See: S.A. Vanstone et al. p. 2118).

Incidentally, Vanstone teaches a variant RSA. Vanstone suggests selecting a random  $e$  (See: Vanstone's *Using four-primes RSA*). As appreciated by the encryption community, this approach does not contribute to expedited cryptography. The opposite is true because a random  $e$  can be as large as  $n$  and exponentiation with such  $e$  can be extremely slow.

Nemo, another one of the cited references, discloses three-prime RSA (i.e., building  $n$  from three primes) and provides a processing time comparison between two-prime and three-prime RSA encryption methods. Ignoring for a moment the fact that Nemo may not qualify as a prior art, Nemo does not teach or suggest each and every element of the invention nor does it enable the invention as described above. Specifically, Nemo does not teach or suggest using at least three prime numbers  $p_1, p_2, \dots, p_k$  from which the modulus  $n$  is provided/computed that are both distinct and random (See: Nemo's Section 4.3). Of course, Nemo fails also to address such features as the parallel processing of sub-tasks and the structural elements of the encryption system (e.g., with exponentiators for parallel processing).

Nemo also does not enable practice of the invention, including the need to use the  $k$  distinct and random prime numbers for establishing  $d$  in the manner as described above. Merely stating that, as a minor benefit,  $n$  can be build from three primes and that the likelihood of a random 256-bit number being prime is greater than the likelihood of a random 384-bit number being prime is not sufficient to enable the present invention (See: Nemo Section 4.3). In order to both teach and enable the present invention all the elements as described above must be found in Nemo. But, as just pointed, Nemo's disclosure is deficient with regard to both criteria for anticipation.

Slavin, the third reference the Examiner relied on for rejecting the claims, discloses a scheme for monitoring compliance of a public key encoding key using differential security levels (See: title, abstract, and claims 1-13 at col. 13-14). In fact, unlike the present invention as recited in claim 1-7 and 9-61, Slavin is not about multi-prime RSA, but rather is about using differential security levels (where unbalanced-RSA happens to be one possible encryption method). Slavin teaches away from using multi-prime in that it recommends against general use



of multi-prime (col. 7 lines 6-8 and 49-53). In stating that for a given  $n$  smaller primes result in less security Slavin fails to appreciate the value of multi-primes in RSA for general use.

Slavin discloses, in col. 7 line 37, preferably "using four [4] randomly selected prime numbers  $p_1, q_1, p_2, q_2$ , all of different values." However, when read in the context of Slavin's entire disclosure, including Slavin's claims, this assertion has a more limited meaning. For example, in col. 3, lines 17-26, Slavin discloses using no more than 4 primes unlike the present invention in which  $k > 2$  can be also  $k > 4$ . Besides, in col. 4, lines 8-13, Slavin discloses that all of the recipient public keys are generated using typically different prime factors that are unlikely to have been selected by another user. In claim 6, Slavin recites "selecting a plurality of prime numbers" without mention of discrete or random. Namely, Slavin does not consider the prime numbers being random and different (discrete) a necessary element, or else Slavin would have recited them this way. In claims 1 and 11, Slavin doesn't even address the plurality of primes. Furthermore, in col. 4, lines 38-60, Slavin discloses that, preferably, the product of the pair of primes  $p_2, q_2$ , is substantially larger than either one of the primes  $p_1, q_1$  (lines 45-51); and that  $p_1, q_1$  are two limited-size factors (lines 38-43).

As mentioned before, it is well settled that for anticipation the reference must teach each and every element of the claimed invention and must be enabling. As shown, the mere mention of four random different primes does not rise to the level of enabling disclosure. This assertion is supported in more than one way by Slavin's disclosure as outlines above. And, unlike the claimed invention wherein it is essential to have  $k$  random distinct prime numbers, the fact that Slavin does require the prime factors to be discrete and random, and in fact places size restrictions on them, teaches away from making this feature an essential element. As such, Slavin's disclosure is non enabling in that it does not avoid undue experimentation, considering the universe of prime numbers, in order to find that only discrete random primes can be employed to exercise the invention and produce the benefits associated with it.

In addition, and no less important, is the fact that Slavin discloses encapsulating the encoded message with the registered public key  $\{n, e, g\}$  before it sent by the sender (See, e.g., col. 7, line 58 to col. 8 line 9, col. 12, lines 9-13). Namely, after the message is encoded with the recipient's public key  $(n, e)$ , but before it is sent by the sender it is encapsulated. Contrast this with the claimed invention according to which the sender does not modify the encoded message

(be is ciphertext or signed message; See, e.g., explanation of the invention in the previous Section XIV).

Slavin also does not teach or suggest, and does not enable, creating the signed message as a function of the private key  $(d,n)$  as recited in claim 9. As well, Slavin does not teach the coefficients or suggest the manner in which such coefficients are used in creating the ciphertext as recited in claim 7. Finally, although this is not an exhaustive comparison, from these examples one could easily understand that the claimed invention is patentably distinguishable from Slavin's teachings. Again, the analysis of Slavin is presented herein notwithstanding the fact that Applicants reserve their right to dispute the use of Slavin as prior art in the first place.

**Itakura**, the next cited reference the Examiner relied on, discloses a scheme for accountable-group multi-signatures as an extension of RSA public key encryption. Namely, Itakura discloses a signature system rather than an encryption system. As shown in Figs. 2 and 3, the conventional cryptographic key is signed by a verifier and further signed by an approver in a scheme somewhat similar to a certificate authority approval. In any event, although in Fig. 1, Itakura shows a random number key generator it also states that of the three prime numbers it uses two are large and one is small (See, e.g., abstract). Indeed, Itakura discloses that there are restrictions placed on the position numbers,  $r_i$ , and shows how to apply such restrictions and find an optimal combination of keys  $p, q, \& r$  (See, page 5, Sections 3.2 & 3.3; e.g., "Therefore,  $r$  should be as small as possible"). In every respect, Itakura does not disclose three more prime numbers that must be random and distinct. Contrast this with the present invention in which  $k$  random distinct prime numbers constitute an essential element. Moreover, the  $r_i$  keys are numbers assigned in order of (organization) hierarchy and are public not private.

In further contrast to the claimed invention, Itakura modifies the encoded message (by the accountable-group signatures) before sending it. Although Itakura discloses generating a signed message using the private key  $d$ , it does not provide an enabling disclosure for creating a ciphertext using the public key  $e$  with multi-primes ( $k > 2$ ). Furthermore, Itakura does not teach using coefficients  $a_e, \dots, a_0$  in creating the ciphertext message in the manner as recited for example in claim 7. As before, this is not an exhaustive comparison but it highlights the fact that the claimed invention is patentably distinguishable from Itakura.

The other references which were cited but not relied on are deemed no more relevant than the foregoing references (Section 71 of the Office Action). Having said all that, and having

shown how the invention is patentably distinguishable over the cited references, it is respectfully submitted that the cited references do not support the claim rejections because they do not teach, suggest or enable the claimed invention.

Then, in further traversing the claim rejections, select comments made by the Examiner in Sections 32-69 of the Office Action are hereafter addressed. It is noted that in Sections 61-69, the Examiner did not treat the claims individually, but rather made comments relating to the specific references, Vanstone, Nemo, Slavin and Itakura, where each of these comments swept at once over the entire group of claims 1-7 and 9-61. Therefore, Applicants primarily rely on the explanation above which more specifically shows why the cited references neither teach nor suggest or enable the claimed invention as recited in claims 1-7 and 9-61.

Secondarily, as to claim 1 the Examiner relies on Rivest and suggests that to apply CRT (Chinese Remainder Theorem) the primes must be relatively primed in pairs, implying their distinctness (Section 33 of the Office Action). However, the Examiner imports this assertion into Rivest in order to attribute the distinct and random character of the primes to Rivest. As a matter of 102 rejection practice this is not allowed in order to provide for the deficiency in Rivest. Besides, the claimed invention is not restricted to CRT as a means for combining the results of the subtasks, when such subtasks are used. Further as to claim 1, the discussion above illustrates how this claim distinguishes over the cited references (Sections, 61-69 of the office Action). Accordingly, it is respectfully submitted that claim 1 is allowable over the cited references.

Noting also the Examiner's comments as to claim 2, Rivest does not disclose nor enable establishing  $d$  as a function of  $n$ ,  $e$  and the  $k$  random and distinct primes. Moreover, as claim 2 includes all the elements of allowable claim 1 it is also allowable over the cited references (Sections 34 and 61-69 of the Office Action).

As to claims 3-6 and 11-12, even if Rivest mentions terminal 1 and terminal 2 it does not meet all the elements of such claims (as outlined above with respect to claims 1, 2, et seq.) The remaining references are deficient as well in view of the explanation above (Sections 35-38, 42-44 and 61-69 of the Office Action).

As to claim 7, Rivest likewise fails to disclose or enable using the  $k$  random and distinct primes. For the reasons as described above, this is true even if Rivest mentions the coefficients  $a_e, \dots, a_0$  (Sections 39-40 and 61-69 of the Office Action).

As to claims 14-61, the foregoing arguments apply with equal force and effect (Sections 45-69 of the Office Action). To recap some of the differences, as to claims 18 and 19, for example, Rivest does not disclose or enable establishing  $d$  as a function of  $n$ ,  $e$  and the  $k$  random and distinct primes (Sections 48, 49). As to claims 20-23 and 50-55, solving the subtasks in accordance with the present invention is not limited to CRT alone and the invention is not claimed with such limitation (Sections 50, 59). This is true even if CRT can produce performance advantage when performed serially; and it is clear that performance of CRT is not inherently parallel as it can be serial as well. Moreover, the structural elements of the encryption system (as recited in claims 45 et seq) and the parallel processing of the sub-tasks is not found in the references (Sections 54-58). As to claims 24-33, Rivest does not disclose or enable the  $k$  random and distinct primes nor does it address the comparison between the respective computation cycles in two-prime and multi-prime encryption schemes (Sections 51, 52). As to claims 34-39, Rivest does not address or suggest using the  $k$  random and distinct primes and does not worry about backward compatibility (Section 53). And, as to claims 56-61, it would not be inherent in Rivest to generate the  $k$  random and distinct primes (Section 60). At the time of Rivest and Vanstone's papers, for example, there was no key development and there is no proof of that in either of them. In fact, they resorted to selecting the primes from a list or databases. The fact that the primes were pre-existing in the list, rather than developed, is an important distinction for the purpose of encryption security. Again, no matter how large the database is, selection from a subset of numbers is not synonymous with selection of a random number. Selection of  $k$  random numbers is characterized in that each of the numbers is equally likely to be selected.

Accordingly, Applicants respectfully submit that claims 1-7 and 9-61 are allowable over the cited references. Reconsideration and withdrawal of the claim rejections under 35 USC 102 are hereby respectfully solicited.

#### **XVI. Double Patenting Rejection Over Co-pending Application**

The Examiner provisionally rejected claims 9, 11, 12, 35 and 50-55 over claims in co-pending Application by the same inventors (09/328,726). The claims as now presented in this Reissue Application are distinguishable from claims 14-62 in the co-pending Application. Accordingly, Applicants believe that a Terminal Disclaimer is not warranted at this time.

Applicants respectfully request that this rejection be reconsidered and withdrawn or at the very least be withheld until issue of one of the Applications as a patent

## **XVII. Conclusion**

### **A. Summary**

Applicants appreciate the Examiner's review of this Reissue Application and respectfully request reconsideration and allowance of the pending claims 1-7 and 9-61 as now presented in view of the foregoing amendments and remarks. Applicants believe that all the objections and rejections have been overcome and that the Reissue Application is in condition for allowance.

### **B. Interview Requested**

If any issues remain unresolved, the Examiner is kindly requested to contact the undersigned Applicants' attorney. Applicants appreciate the opportunity to discuss such issues with the Examiner in order to expedite the examination of this Reissue Application.

### **C. Fee Authorization:**

If for any reason an insufficient fee has been paid, the Commissioner is hereby authorized to charge any deficiency in payment of required fees associated with this communication to Deposit Account 02-3964.

Date: September 9, 2002

Respectfully submitted,



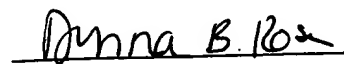
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#### **CERTIFICATE OF MAILING (37 CFR 1.8)**

I hereby certify that this correspondence (along with all referenced and attached papers) is being deposited with the U.S. Postal Service in an envelop with sufficient postage as first class mail addressed to Box Reexam Patent Application, Assistant Commissioner for Patents, Washington, D.C. 20231, on

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24. (New) Amended) The method according to claim 20, 21,  
wherein  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein the deciphering the number  $C$  to derive the number  $M$  is divided into subtasks, one  
subtask for each of the  $k$  distinct random prime numbers,  
wherein the  $k$  distinct random prime numbers are each smaller than  $p$  and  $q$ ,  
whereby for a given length of  $n$  it takes fewer computational cycles to ~~find and check the  $K$~~   
~~distinct random prime numbers that it takes to find and check~~perform the deciphering  
relative to the number of computational cycles for performing such deciphering if the pair  
of prime numbers  $p$  and  $q$  were used instead.

25. (New) Amended) The method according to claim 22,  
wherein  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein the deciphering the number  $C$  to derive the number  $M$  is divided into subtasks, one  
subtask for each of the  $k$  distinct random prime numbers,  
wherein the  $k$  distinct random prime numbers are each smaller than  $p$  and  $q$ ,  
whereby for a given length of  $n$  it takes fewer computational cycles to ~~find and check the  $K$~~   
~~distinct random prime numbers that it takes to find and check~~perform the deciphering relative to  
the number of computational cycles for performing such deciphering if the pair of prime  
numbers  $p$  and  $q$  were used instead.

26. (New) Amended) The method according to claim 24, 20,  
wherein ~~the~~ $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein developing the at least three distinct random prime numbers and computing steps can  
ben is performed, including for  $n$  that is more than 600 digits long faster, in less time than  
heretofore possible with only it takes to develop the pair of prime numbers  $p$  and  $q$  and compute  
that  $n$ .

27. (New) Amended) The method according to claim 25, 22,  
wherein ~~the~~ $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and

wherein developing, the at least three distinct random prime numbers and computing and encoding steps can be performed, including for  $n$  that is more than 600 digits long faster, in less time than heretofore possible with only it takes to develop the pair of prime numbers  $p$  and  $q$  and compute that  $n$ .

28. (New) Amended The method according to claim 14,  
wherein  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein the deciphering step is divided into sub-steps, one sub-step for each of the  $k$  distinct random prime numbers,  
wherein the  $k$  distinct random prime numbers are each smaller than  $p$  and  $q$ ,  
whereby for a given length of  $n$  it takes fewer computational cycles to ~~find and check the  $K$  distinct random prime numbers that it takes to find and check~~perform the deciphering step relative to the number of computational cycles for performing such deciphering step if the pair of prime numbers  $p$  and  $q$  were used instead.

29. (New) Amended The method according to claim ~~28~~, 14,  
wherein ~~the~~  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein developing the  $k$  distinct random prime numbers and computing steps can be the composite number  $n$  are performed, including for  $n$  that is more than 600 digits long faster, in less time than heretofore possible with only it takes to develop the pair of prime numbers  $p$  and  $q$  and compute that  $n$ .

30. (New) Amended The method according to claim 16,  
wherein  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein the decoding step is divided into sub-steps, one sub-step for each of the  $k$  distinct random prime numbers,  
wherein the  $k$  distinct random prime numbers are each smaller than  $p$  and  $q$ ,  
whereby for a given length of  $n$  it takes fewer computational cycles to ~~find and check the  $K$  distinct random prime numbers that it takes to find and check~~perform the decoding step relative

to the number of computational cycles for performing such decoding step if the pair of prime numbers  $p$  and  $q$  were used instead.

31. (New)-Amended) The method according to claim 30, 16,  
wherein ~~the~~  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , and  
wherein developing the  $k$  distinct random prime numbers and computing steps ~~can be~~ the  
composite  $n$  is performed, including for  $n$  that is more than 600 digits long faster, in less time  
than heretofore possible with only it takes to develop the pair of prime numbers  $p$  and  $q$  and  
compute that  $n$ .

32. (New)-Amended) The method according to claim 18,  
wherein  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , ~~and~~  
wherein the encoding step is divided into sub-steps, one sub-step for each of the  $k$  distinct  
random prime numbers,  
wherein the  $k$  distinct random prime numbers are each smaller than  $p$  and  $q$ ,  
whereby for a given length of  $n$  it takes fewer computational cycles to ~~find and check the  $K$~~   
~~distinct random prime numbers that it takes to find and check~~ perform the encoding step relative  
to the number of computational cycles for performing such encoding step if the pair of prime  
numbers  $p$  and  $q$  were used instead.

33. (New)-Amended) The method according to claim ~~32~~, 18,  
wherein ~~the~~  $p$  and  $q$  are a pair of prime numbers the product of which equals  $n$ , ~~and~~  
wherein developing the  $k$  distinct random prime numbers and computing steps ~~can be~~ the  
composite number  $n$  is performed, including for  $n$  that is more than 600 digits long faster, in less  
time than heretofore possible with only it takes to develop the pair of prime numbers  $p$  and  $q$  and  
compute that  $n$ .

34. (New)Amended) The method according to claim 14, wherein a message cryptographically  
processed in accordance with ~~by~~ the method is compatible ~~sender~~ with two-prime RSA public key  
cryptographycryption characterized by  $n$  being equal to a composite number computed as the



product of 2 prime numbers  $p$  and  $q$ , is decipherable with multi-prime ( $k > 2$ ) RSA public key encryption characterized by the composite number  $n$  being computed as the product of the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ .

35. (New Amended) The method according to claim 14,9, wherein at the signed message word signal  $M_s$ , formed from the digital message word signal  $M_l$  being cryptographically processed in accordance at the first terminal with the method multi-prime ( $k > 2$ ) RSA public key encryption which is compatible characterized by the composite number  $n$  being computed as the product of the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , is decipherable at the second terminal with two-prime RSA public key cryptography encryption characterized by  $n$  being equal to a composite number computed as the product of 2 prime numbers  $p$  and  $q$ .

36. (New Amended) The method according to claim 16, wherein a message cryptographically processed in accordance with by the method is compatible sender with two-prime RSA public key cryptography encryption characterized by  $n$  being equal to a composite number computed as the product of 2 prime numbers  $p$  and  $q$ , is decipherable by the decoding with multi-prime ( $k > 2$ ) RSA public key encryption characterized by the composite number  $n$  being computed as the product of the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ .

37. (New Amended) The method according to claim 18, wherein at the signed message  $M_s$ , formed from the plaintext message data  $M$  being cryptographically processed in accordance at the sender with the method multi-prime ( $k > 2$ ) RSA public key encryption which is compatible characterized by the composite number  $n$  being computed as the product of the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , is decipherable by the decoding at the recipient with two-prime RSA public key cryptography encryption characterized by  $n$  being equal to a composite number computed as the product of 2 prime numbers  $p$  and  $q$ .

38. (New Amended) The method according to claim 20, wherein a message data cryptographically processed in accordance with by the method is compatible sender with two-prime RSA public key cryptography encryption characterized by  $n$  being equal to a composite

number computed as the product of 2 prime numbers  $p$  and  $q$ , is decipherable at the recipient with multi-prime RSA public key encryption characterized by the composite number  $n$  being computed as the product of the at least three distinct random prime numbers.

39. (NewAmended) The method according to claim 22, wherein a message data cryptographically processed in accordance with by the method is compatible sender with two-prime RSA public key cryptography encryption characterized by  $n$  being equal to a composite number computed as the product of 2 prime numbers  $p$  and  $q$ , is decipherable at the recipient with multi-prime RSA public key encryption characterized by the composite number  $n$  being computed as the product of the at least three distinct random prime numbers.

40. (NewAmended) A cryptography method for local storage of data by a private key owner, comprising the steps of:

selecting a public key portion  $e$ ;

developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots, p_k-1$ , is relatively prime to the public key portion  $e$ ;

establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the form of

$$d \equiv e^{-1} \pmod{(p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1)};$$

computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers that are factors of  $n$ , where only the private key owner knows the factors of  $n$ ; and

encoding plaintext data  $M$  to ciphertext data  $C$  for the local storage, using a relationship of the form  $C \equiv M^e \pmod{n}$ , where  $0 \leq M \leq n-1$ , whereby the ciphertext data  $C$  is decipherable only by the private key owner having available to it the factors of  $n$ .

41. (New) The cryptography method in accordance with claim 40, further comprising the step of:

decoding the ciphertext data  $C$  from the local storage to the plaintext data  $M$  using a relationship of the form  $M \equiv C^d \pmod{n}$ .

42. (New Amended) A cryptographic communications system, comprising:  
a plurality of stations;  
a communications medium; and  
a host system adapted to ~~conduct encrypted communications~~ communicate with the plurality of stations via the communications medium sending a receiving messages cryptographically processed with an RSA public key encryption, the host system including

at least one cryptosystem ~~responsive to encryption and/or decryption requests from the~~

~~host system, the cryptosystem being configured for~~

~~developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ ,~~

~~checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots$~~

~~$p_k-1$ , is relatively prime to a public key portion  $e$  that is associated with the host system,~~

~~computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers,~~

~~establishing a private key portion  $d$  by a relationship to the public key portion  $e$~~

~~in the form of  $d \equiv e^{-1}(\text{mod}((p_1-1) \cdot (p_2-1) \cdots (p_k-1)))$ ,~~

~~in response to an encoding request from the host system, encoding a plaintext~~

~~message data  $M$  producing therefrom a ciphertext message data  $C$  to be~~

~~communicated via the host system, the encoding using a relationship of~~

~~the form  $C \equiv M^e (\text{mod } n)$ , where  $0 \leq M \leq n-1$ ,~~

~~establishing a private key portion  $d$  by a relationship to the public key portion  $e$~~

~~in the form of ; and~~

~~in response to a decoding request from the host system, decoding a ciphertext~~

~~message data  $C'$  communicated via the host producing therefrom a~~

~~plaintext message data  $M'$  using a relationship of the form  $M' \equiv C'^d (\text{mod } n)$ , where  $C'$  and  $M'$  can be respectively  $C$  and  $M$ .~~

43. (New Amended) A system for ~~processing a message used in cryptographic~~  
~~communications of a message cyptographically processed with RSA public key encryption,~~  
comprising:

a bus; and

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a cryptosystem ~~operatively~~communicatively coupled to and receiving from the bus  
~~encryption~~encoding and ~~decryption~~decoding requests, the cryptosystem being  
~~capable~~configured ~~effor~~  
 providing a public key portion  $e$ ,  
 developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ ,  
 checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots, p_k-1$ ,  
 is relatively prime to the public key portion  $e$ ,  
 computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers,  
 encoding a plaintext form of a first message  $M$  to produce a ciphertext form of the first  
 message  $C$  using a relationship of the form  $C \equiv M^e \pmod{n}$ , where  $0 \leq M \leq n-1$ ,  
 establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the  
 form of  $d \equiv e^{-1} \pmod{((p_1-1) \cdot (p_2-1) \cdots (p_k-1))}$ ,  
in response to an encoding request from the bus, encoding a plaintext form of a first  
message  $M$  to produce  $C$ , a ciphertext form of the first message, using a  
relationship of the form  $C \equiv M^e \pmod{n}$ , where  $0 \leq M \leq n-1$ , and  
in response to an decoding request from the host system, decoding  $C'$ , a ciphertext form  
of a second message  $C'$ , to produce the  $M'$ , a plaintext form of the second message  
 $M'$ , using a relationship of the form  $M' \equiv C'^d \pmod{n}$ , the first and second  
messages can be being distinct or one and the same.

44. (New) The system of claim 42, wherein the at least one cryptosystem includes  
 a plurality of exponentiators configured to operate in parallel in developing respective  
 subtask values corresponding to the message.

45. (New Amended) The system of claim 42, wherein the at least one cryptosystem includes  
 a processor,  
 a data-address bus,  
 a memory-operatively coupled to the processor via the data-address bus,  
 a data encryption standard (DES) unit operatively-coupled the memory and the processor  
 via the data-address bus,

a plurality of exponentiator elements ~~operatively~~ coupled to the processor via the DES unit, the plurality of exponentiator elements being configured to operate in parallel in developing respective subtask values corresponding to the message.

46. (New Amended) The system of claim 45, wherein the memory and each of the plurality of exponentiator elements has its own DES unit that ~~encrypts~~ cryptographically processes message data received/returned from/to the processor.

47. (New Amended) The system of claim 45, wherein the memory is partitioned into address spaces addressable by the processor, including secure, insecure and exponentiator elements address spaces, and wherein the DES unit ~~that is coupled to the processor is~~ configured to recognize the secure and exponentiator elements address spaces and to automatically ~~encrypt~~ encode message data therefrom before it is provided to the exponentiator elements, the DES unit being bypassed when the processor is accessing the insecure memory address spaces, the DES unit being further configured to ~~decrypt~~ decode ~~encrypted~~ encoded message data received from the memory before it is provided to the processor.

48. (New) The system of claim 45, wherein the at least one cryptosystem meets FIPS (Federal Information Processing Standard) 140-1 level 3.

49. (New) The system of claim 45, wherein the processor maintains in the memory the public key portion  $e$  and the composite number  $n$  with its factors  $p_1, p_2, \dots, p_k$ .

50. (New Amended) A system for ~~processing a message used in cryptographic communications of a message cryptographically processed with RSA public key encryption,~~ comprising:

a bus; and

a cryptosystem receiving from the system via the bus ~~encryption~~ encoding and ~~decryption~~ decoding requests, the cryptosystem including a plurality of exponentiator elements configured to develop subtask values,

a memory, and

a processor configured for

receiving the ~~encryption~~encoding and ~~decryption~~decoding requests, each ~~encryption~~encoding request providing a plaintext message  $M$  to be ~~encrypted~~encoded, ~~each encryption request can additionally provide~~ obtaining a public key that includes an exponent  $e$  and a modulus  $n$ , a representation of ~~the~~ modulus  $n$  existing in the memory in the form of its  $k$  distinct random prime number factors  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , ~~or the processor can obtain the public key from the memory,~~ constructing subtasks, one subtask for each of the  $k$  factors, to be executed by the exponentiator elements for producing respective ones of the subtask values,  $C_1, C_2, \dots, C_k$ , and forming a ciphertext message  $C$  from the subtask values  $C_1, C_2, \dots, C_k$ , wherein the ciphertext message  $C$  is decipherable using a private key that includes the modulus  $n$  and an exponent  $d$  which is a function of  $e$ .

51. (New~~Amended~~) The system of claim 50 wherein each one of the subtasks  $C_1, C_2, \dots, C_k$  is developed using a relationship of the form  $C_i \equiv M_i^{e_i} \pmod{p_i}$ , where  $M_i \equiv M \pmod{p_i}$ , and  $e_i \equiv e \pmod{p_i - 1}$ , and where  $i=1, 2, \dots, k$ .

52. (New~~Amended~~) A system for ~~processing a message used in cryptographic communications~~ of a message cryptographically processed with RSA public key encryption, comprising:

a bus; and

a cryptosystem receiving from the system via the bus ~~encryption~~encoding and ~~decryption~~decoding requests, the cryptosystem including a plurality of exponentiator elements configured to develop subtask values, a memory, and a processor configured for

receiving the ~~encryption~~encoding and ~~decryption~~decoding requests, each ~~encryption/decryption~~encoding/decoding request ~~providing~~provided with a plaintext/ciphertext message  $M/C$  to be ~~encrypted/decrypted~~encoded/decoded and can additionally ~~provide~~with or ~~without~~ a public/private key that includes an exponent  $e/d$  and a modulus  $n$  ~~a representation of a modulus  $n$  which exists in the memory~~ in the form of its  $k$  distinct random prime number factors  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , ~~or the processor can obtain~~  
~~obtaining~~ the public/private key from ~~the memory~~, the memory if the encoding/decoding request is provided without the public/private key, constructing subtasks to be executed by the exponentiator elements for producing respective ones of the subtask values,  $M_1, M_2, \dots, M_k/C_1, C_2, \dots, C_k$ , and forming the ciphertext/plaintext message  $C/M$  from the subtask values  $C_1, C_2, \dots, C_k/M_1, M_2, \dots, M_k$ .

53. (New Amended) The system of claim 52 wherein when produced each one of the subtasks  $C_1, C_2, \dots, C_k$  is developed using a relationship of the form  $C_i \equiv M_i^{e_i} \pmod{p_i}$ , where  $C_i \equiv C \pmod{p_i}$ , and  $e_i \equiv e \pmod{p_i - 1}$ , and where  $i=1, 2, \dots, k$ .

54. (New Amended) The system of claim 52 wherein when produced each one of the subtasks  $M_1, M_2, \dots, M_k$  is developed using a relationship of the form  $M_i \equiv C_i^{d_i} \pmod{p_i}$ , where  $M_i \equiv M \pmod{p_i}$ , and  $d_i \equiv d \pmod{p_i - 1}$ , and where  $i=1, 2, \dots, k$ .

55. (New) —The system of claim 54, wherein the private key exponent  $d$  relates to the public key exponent  $e$  via  $d \equiv e^{-1} \pmod{((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1))}$ .

56. (New Amended) A system for ~~processing a message used in cryptographic communications~~ of a message cryptographically processed with RSA public key encryption, comprising:

means for selecting a public key portion  $e$ ;

means for developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and for checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots, p_k-1$ , is relatively prime to the public key portion  $e$ ;

means for establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the form of  $d \equiv e^{-1}(\text{mod}((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1)))$ ;

means for computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers;

means for ~~obtaining~~receiving a ciphertext message data  $C$ ; and

means for decoding the ciphertext message data  $C$  to a plaintext message data  $M$  using a relationship of the form  $M \equiv C^d (\text{mod } n)$ .

57. (New) The system according to claim 56, further comprising:

means for encoding the plaintext message data  $M$  to the ciphertext message data  $C$ , using a relationship of the form  $C \equiv M^e (\text{mod } n)$ , where  $0 \leq M \leq n-1$ .

58. (New (Amended)) A system for ~~processing a message used in cryptographic communications of a message cryptographically processed with RSA public key encryption,~~ comprising:

means for selecting a public key portion  $e$ ;

means for developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and for checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots, p_k-1$ , is relatively prime to the public key portion  $e$ ;

means for establishing a private key portion  $d$  by a relationship to the public key portion  $e$  of the form  $d \equiv e^{-1}(\text{mod}((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1)))$ ;

means for computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers; and



means for encoding a plaintext message data  $M$  with the private key portion  $d$  to produce a signed message  $M_s$ , using a relationship of the form  $M_s \equiv M^d \pmod{n}$ , where  $0 \leq M \leq n-1$ , the signed message  $M_s$  being decipherable using the public key portion  $e$ .

59. (New Amended) The system of claim 58 further comprising the step of:  
means for decoding the signed message  $M_s$  with the ~~private~~public key portion  $e$  to produce the plaintext message data  $M$  using a relationship of the form  $M \equiv M_s^e \pmod{n}$ .

60. (New Amended) The system of claim 57, wherein the system can ~~conduct encrypted communications with other public key cryptography~~communicate the cryptographically processed message to another system that encrypt/encodes/decrypt/decodes data with RSA public key encryption using a modulus value equal to  $n$  independent of the  $k$  distinct prime numbers.

61. (New) Amended) The system of claim 59, wherein the system can ~~conduct encrypted communications~~communicate the cryptographically processed message to another system that encodes/decodes data with other RSA public key cryptography systems that encrypt/decrypt dataencryption using a modulus value equal to  $n$  independent of the  $k$  distinct prime numbers.

Document comparison done by DeltaView on Monday, August 26, 2002 08:45:01

Input:	
Document 1	pdocs://siliconvalley/266556/1
Document 2	pdocs://siliconvalley/266555/1
Rendering set	Standard

Legend:	
<u>Insertion</u>	
<u>Deletion</u>	
<u>Moved from</u>	
<u>Moved to</u>	
<u>Format change</u>	
<u>Moved deletion</u>	
Inserted cell	
Deleted cell	
Moved cell	
Split/Merged cell	
Padding cell	

Statistics:	
	Count
Insertions	407
Deletions	326
Moved from	4
Moved to	4
Format changed	0
Total changes	741

File Compare Results to Show Changes to the Claims Since the Preliminary Amendment

Clean version of the Claims

*Clean version of the claims with all of the changes to be made vis-à-vis the U.S. Patent 5,848,159, as follows:*

1. (Twice Amended) A method of ~~processing a message for use in cryptographic communications of a message cryptographically processed with RSA (Rivest, Shamir & Adleman) public key encryption,~~ comprising the steps of:

developing  $k$  distinct random prime numbers  $p_1, p_2, \dots, p_k$ , where  $k$  is an integer greater than 2;

providing a number  $e$  relatively prime to  $(p_1 - 1) \cdot (p_2 - 1) \cdot \dots \cdot (p_k - 1)$ ;

providing a composite number,  $n$ , as a equaling the product of  $p_1 \cdot p_2 \cdot \dots \cdot p_k$  where  $k$  is an integer greater than 2, and  $p_1, p_2, \dots, p_k$  are distinct random prime numbers; and;

receiving a ciphertext word signal  $C$  which is formed by encoding a plaintext message word signal  $M$  to a ciphertext word signal  $C$ , where  $M$  corresponds to a number representative of the message and

$$0 \leq M \leq n-1,$$

where  $C$  is a number representative of an encoded form of the plaintext message word signal  $M$  such that

$C \equiv M^e \pmod{n}$ , and where  $e$  is associated with an intended recipient of the ciphertext word signal  $C$ ; and

where  $e$  is a number relatively prime to  $(p_1 - 1) \cdot (p_2 - 1) \cdot \dots \cdot (p_k - 1)$ .

deciphering the received ciphertext word signal  $C$  at the intended recipient having available to it the  $k$  distinct random prime numbers  $p_1, p_2, \dots, p_k$ .

2. (Twice Amended) The method according to claim 1, comprising wherein the further deciphering step of: includes

establishing a number,  $d$ , as a multiplicative inverse of

$$e \pmod{\text{lcm}((p_1 - 1), (p_2 - 1), \dots, (p_k - 1))}; \text{ and}$$

decoding the ciphertext word signal  $C$  to the plaintext message word signal  $M$  where  
 $M \equiv C^d \pmod{n}$ .

3. (Twice Amended) A method for communications of processing a message signal  $M_i$  for use cryptographically processed with RSA public key encryption in a communications system having  $j$  terminals, each terminal being characterized by an encoding key  $E_i = (e_i, n_i)$  and a decoding key  $D_i = (d_i, n_i)$ , where  $i=1, 2, \dots, j$ , and the message signal  $M_i$  ~~corresponding~~ corresponds to a number representative of a message-to-be-transmitted received from the  $i^{\text{th}}$  terminal, the method comprising the steps of:

~~computing~~ establishing  $n_i$  where  $n_i$  is a composite number of the form

$$n_i = p_{i,1} \cdot p_{i,2} \cdot \dots \cdot p_{i,k}$$

where  $k$  is an integer greater than 2,

$p_{i,1}, p_{i,2}, \dots, p_{i,k}$  are distinct random prime numbers,

$e_i$  is relatively prime to  $\text{lcm}(p_{i,1}-1, p_{i,2}-1, \dots, p_{i,k}-1)$ , and

$d_i$  is selected from the group consisting of the class of numbers equivalent to a multiplicative inverse of

$$e_i \pmod{\text{lcm}((p_{i,1}-1), (p_{i,2}-1), \dots, (p_{i,k}-1))};$$

receiving by a recipient terminal ( $i=y$ ) from a sender terminal ( $i=x, x \neq y$ ) a ciphertext signal  $C_x$  formed by encoding a digital message word signal  $M_1$  for transmission from a first terminal ( $i=1$ ) to a second terminal ( $i=2$ )  $M_x$ , said encoding step including wherein the sub-step of: encoding includes

transforming said message word signal  $M_1 M_x$  to one or more message block word signals

$M_1 M_x$ ", each block word signal  $M_1 M_x$ " corresponding to a number representative of a portion of said message word signal  $M_1 M_x$  in the range  $0 \leq M_1 M_x \leq n_2 - 1, n_y - 1$ , and

transforming each of said message block word signals  $M_1 M_x$ " to a ciphertext word signal

$C_1 C_x$  that corresponds to a number representative of an encoded form of said message block word signal  $M_1 M_x$ " where

$$C_x \equiv M_x^{e_y} \pmod{n_y}; \text{ and}$$

deciphering the received ciphertext word signal  $C_x$  at the recipient terminal having available to it the  $k$  distinct random prime numbers  $p_{y,1}, p_{y,2}, \dots, p_{y,k}$  for establishing its  $d_y$ .

4. (Twice Amended) A cryptographiesystem for communications systemof a message cryptographically processed with an RSA public key encryption, comprising:

a communication channel adapted for transmitting a ciphertext word signal  $C$  that relates to a transmit message word signal  $M$ ;

encoding means coupled to said channel and adapted for transforming thea transmit message word signal  $M$  to the ciphertext word signal  $C$  using a composite number,  $n$ , where  $n$  is a product of the form

$$n = p_1 \cdot p_2 \cdot \dots \cdot p_k$$

$k$  is an integer greater than 2, and

$p_1, p_2, \dots, p_k$  are distinct random prime numbers,

where the transmit message word signal  $M$  corresponds to a number representative of athe message and

$$0 \leq M \leq n-1$$

where the ciphertext word signal  $C$  corresponds to a number representative of an encoded form of said message through a relationship of the form{and corresponds to}

$$C \equiv M^e \pmod{n}, \text{ and}$$

where  $e$  is a number relatively prime to  $\text{lcm}(p_1 - 1, p_2 - 1, \dots, p_k - 1)$ ; and

decoding means coupled to said channel and adapted for receiving the ciphertext word signal  $C$  from said channel and, having available to it the  $k$  distinct random prime numbers  $p_1, p_2, \dots, p_k$ , for transforming the ciphertext word signal  $C$  to a receive message word signal  $M'$  where  $M'$  corresponds to a number representative of a decoded form of the ciphertext word signal  $C$  through a relationship of the form

$$M' \equiv C^d \pmod{n}$$

where  $d$  is selected from the group consisting of a class of numbers equivalent to a multiplicative inverse of

$$e(\text{mod}(\text{lcm}((p_1 - 1), (p_2 - 1), \dots, (p_k - 1)))).$$

5. (Twice Amended) A cryptographiesystem for communications of a message  
cryptographically processed with an RSA public key encryption, the system having a plurality of  
 terminals coupled by a communications channel, comprising:

a first terminal of the plurality of terminals characterized by an encoding key

$E_A = (e_A, n_A)$  and a decoding key  $D_A = (d_A, n_A)$ ,

where  $n_A$  is a composite number of the form

$$n_A = p_{A,1} \cdot p_{A,2} \cdot \dots \cdot p_{A,k}$$

where

$k$  is an integer greater than 2,

$p_{A,1}, p_{A,2}, \dots, p_{A,k}$  are distinct random prime numbers,

$e_A$  is relatively prime to

$\text{lcm}(p_{A,1} - 1, p_{A,2} - 1, \dots, p_{A,k} - 1)$ , and

$d_A$  is selected from the group consisting of the class of numbers equivalent to a  
 multiplicative inverse of

$$e_A (\text{mod}(\text{lcm}((p_{A,1} - 1), (p_{A,2} - 1), \dots, (p_{A,k} - 1)))); \text{ and}$$

a second terminal of the plurality of terminals having

blocking means for transforming a first message, which is to be transmitted on  
 said communications channel from said second terminal to said first terminal,  
 to into one or more transmit message word signals  $M_B$ , where each  $M_B$   
 corresponds to a number representative of said first message in the range

$$0 \leq M_B \leq n_A - 1,$$

encoding means coupled to said channel and adapted for transforming each  
 transmit message word signal  $M_B$  to a ciphertext word signal  $C_B$  that  
 corresponds to a number representative of an encoded form of said first message  
through message through a relationship of the form

$$C_B \equiv M_B^{e_A} (\text{mod } n_A),$$

said first terminal having

decoding means coupled to said channel and adapted for receiving each of said ciphertext word signals  $C_B$  from said channel and, having available to it the  $k$  distinct random prime numbers  $p_{A,1}, p_{A,2}, \dots, p_{A,k}$  for transforming each of said ciphertext word signals  $C_B$  to a receive message word signal  $M'_B$ , and means for transforming said receive message word signal  $M'_B$  to said first message, where  $M'_B$  corresponds to a number representative of a decoded form of  $C_B$  through a relationship of the form

$$M'_B \equiv C_B^{d_A} \pmod{n_A}.$$

6. (Twice Amended) The system according to claim 5 wherein said second terminal is characterized by an encoding key  $E_B = (e_B, n_B)$  and a decoding key  $D_B = (d_B, n_B)$ , where  $n_B$  is a composite number of the form

$$n_B = p_{B,1} \cdot p_{B,2} \cdot \dots \cdot p_{B,k}$$

where  $k$  is an integer greater than 2,

$p_{B,1}, p_{B,2}, \dots, p_{B,k}$  are distinct random prime numbers,

$e_B$  is relatively prime to

$\text{lcm}(p_{B,1}-1, p_{B,2}-1, \dots, p_{B,k}-1)$ , and

$d_B$  is selected from the group consisting of a class of numbers equivalent to a multiplicative inverse of

$$e_B \pmod{(\text{lcm}((p_{B,1}-1), (p_{B,2}-1), \dots, (p_{B,k}-1)))},$$

said first terminal further having

blocking means for transforming a second message, [-to-be-transmitted] which is to be transmitted on said communications channel from said first terminal to said second terminal, to one or more transmit message word signals  $M_A$ , where each  $M_A$  corresponds to a number representative of said message in the range

$$0 \leq M_A \leq n_B - 1$$

encoding means coupled to said channel and adapted for transforming each transmit message word signal  $M_A$  to a ciphertext word signal  $C_A$  and for transmitting  $C_A$  on said channel, where  $C_A$  corresponds to a number

representative of an encoded form of said second message through a relationship of the form

$$C_A \equiv M_A^{e_a} \pmod{n_B}$$

said second terminal further having

decoding means coupled to said channel and adapted for receiving each of said ciphertext word signals  $C_A$  from said channel and, having available to it the k distinct random prime numbers  $p_{B,1}, p_{B,2}, \dots, p_{B,k}$  for transforming each of said ciphertext word signals to a receive message word signal  $M'_A$ , and means for transforming said receive message word signals  $M'_A$  to said second message, where  $M'_A$  corresponds to a number representative of a decoded form of  $C_A$  through a relationship of the form

$$M'_A \equiv C_A^{d_a} \pmod{n_B}.$$

7. (Amended) A method of ~~processing a message for use in cryptographic communications of a~~ message cryptographically processed with an RSA public key encryption, comprising the steps of:

developing k factors of a composite number,  $n$ , ~~as a product of at least 3 whole number factors greater than one, the k factors being distinct random prime numbers; and k is an integer larger than two ( $k > 2$ );~~

providing a number e relatively prime to a lowest common multiplier of the k factors;

providing the composite number n;

receiving a ciphertext word signal C which is formed by encoding a digital message word signal M to a ciphertext word signal C, where said digital message word signal M corresponds to a number representative of a said message and

$$0 \leq M \leq n-1,$$

where said ciphertext word signal C corresponds to a number representative of an encoded form of said message through a relationship of the form

$$C \equiv a_e M^e + a_{e-1} M^{e-1} + \dots + a_0 \pmod{n}$$

where e and  $a_e, a_{e-1}, \dots, a_0$  are numbers; and



deciphering the received chiphertext word signal C at an intended recipient with knowledge of the k factors.

8. (Amended) A method according to claim 7 wherein said encoding step further includes the step of

~~transforming said digital message word signal M to said ciphertext word signal C by the performance of a first ordered succession of invertible operations on M, and wherein the method further comprises the step of:~~

~~decoding said ciphertext word signal C to said digital message word signal M by the performance of a second ordered succession of invertible operations on C, where each of the invertible operations of said second ordered succession is the inverse of a corresponding one of said first ordered succession, and where the order of said invertible operations in said second ordered succession is reversed with respect to the order of corresponding invertible operations in said first ordered succession.~~

8. Cancelled.

9. (Twice Amended) A communication system for processing communications of message signals cryptographically processed with RSA public key encryption, comprising:

j terminals including first and second terminals, each of the j terminals being characterized by an encoding key  $E_i = (e_i, n_i)$  and decoding key  $D_i = (d_i, n_i)$ , where  $i=1, 2, \dots, j$ , each of the j terminals being adapted to transmit a particular one of the message signals where an  $i^{\text{th}}$  terminal corresponds to an  $i^{\text{th}}$  message signal  $M_i$  is transmitted from an  $i^{\text{th}}$  terminal, and

$$0 \leq M_i \leq n_i - 1,$$

$n_i$  being a composite number of the form

$$n_i = p_{i,1} \cdot p_{i,2} \cdot \dots \cdot p_{i,k}$$

where

k is an integer greater than 2,

$p_{i,1}, p_{i,2}, \dots, p_{i,k}$  are distinct random prime numbers,

$e_i$  is relatively prime to

$\text{lcm}(p_{i,1}-1, p_{i,2}-1, \dots, p_{i,k}-1)$ , and

$d_i$  is selected from the group consisting of the class of numbers equivalent to a multiplicative inverse of

$e_i \pmod{\text{lcm}((p_{i,1}-1), (p_{i,2}-1), \dots, (p_{i,k}-1))}$ ;

said first terminal including

means for encoding a digital message word signal  $M_1$  to be transmitted from said first terminal ( $i=1$ ) to said second terminal ( $i=2$ ), said encoding means transforming said digital message word signal  $M_1$  to a signed message word signal  $M_{1s}$  using a relationship of the form

~~10. (Amended) The communication system of claim 9 further comprising:~~

~~$M_{1s} \equiv M_1^{d_1} \pmod{n_1}$ ; and~~

~~means for transmitting said signed message word signal  $M_{1s}$  from said first terminal to said second terminal, wherein said second terminal including~~

~~means for decoding said signed message word signal  $M_{1s}$  to said digital message word signal  $M_{1d}$~~

10. (Twice Amended) The system of claim 9, wherein the means for decoding said signed message word signal  $M_{1s}$  includes means for transforming said signed message word signal  $M_{1s}$  using a relationship of the form

$$M_1 \equiv M_{1s}^{e_1} \pmod{n_1}.$$

11. (Twice Amended) A communications system for transferring a message signal cryptographically processed with RSA public key encryption, the communications system comprising:

$j$  communication stations including first and second stations, each of the  $j$  communication stations being characterized by an encoding key  $E_i=(e_i, n_i)$  and a decoding key  $D_i=(d_i,$

$n_i$ ), where  $i=1, 2, \dots, j$ , each of the  $j$  communication stations being adapted to transmit a particular one of the message signals where an  $i^{\text{th}}$  message signal  $M_i$  is received from an  $i^{\text{th}}$  communication station ~~corresponds to an  $i^{\text{th}}$  message signal  $M_i$~~ , and

$$0 \leq M_i \leq n_i - 1$$

$n_i$  being a composite number of the form

$$n_i = p_{i,1} \cdot p_{i,2} \cdot \dots \cdot p_{i,k}$$

where

$k$  is an integer greater than 2,

$p_{i,1}, p_{i,2}, \dots, p_{i,k}$  are distinct random prime numbers,

$e_i$  is relatively prime to  $\text{lcm}(p_{i,1} - 1, p_{i,2} - 1, \dots, p_{i,k} - 1)$ , and

$d_i$  is selected from the group consisting of the class of numbers equivalent to a  
multiplicative inverse of

$$e_i \pmod{(\text{lcm}((p_{i,1} - 1), (p_{i,2} - 1), \dots, (p_{i,k} - 1)))},$$

said first station including

means for encoding a digital message word signal  $M_1$  to be transmitted  
from said first station ( $i=1$ ) to said second station ( $i=2$ ),

means for transforming said digital message word signal  $[M_A] M_1$  to one  
or more message block word signals  $[M_A'] M_1''$ , each block word  
signal  $[M_A'] M_1''$  being a number representative of a portion of said  
message word signal  $M_1$  in the range

$$0 \leq M_1'' \leq n_2 - 1, \text{ and}$$

means for transforming each of said message block word signals  $M_1''$  to a  
ciphertext word signal  $C_1$  using a ~~relationship~~relationship of the form

12. (Amended) ~~The communications system of claim 11 further comprising:~~

$$C_1 \equiv M_1''^{e_2} \pmod{n_2}; \text{ and}$$

means for transmitting said ciphertext word signals  $C_1$  from said first station to said second station, wherein said second station includes

means for deciphering said ciphertext word signals  $C_1$  using  $p_{2,1}, p_{2,2}, \dots, p_{2,k}$  to produce said message word signal  $M_1$ .

12. (Twice Amended) The communications system of claim 11, wherein the deciphering means includes

means for decoding said ciphertext word signals  $C_1$  to said message block word signals  $M_1''$  using a relationship of the form

$$M_1'' \equiv C_1^{d_2} \pmod{n_2}, \text{ and}$$

means for transforming said message block word signals  $M_1''$  to said message word signal  $M_1$ .

13. (Twice Amended) A system for communications system of a message cryptographically processed with RSA public key encryption, comprising:

a first station; and

a second station communicatively connected to the first station ~~for communications therebetween,~~

~~the first communicating station having~~

the first station having

encoding means for transforming a transmit message word signal  $M$  to a ciphertext word signal  $C$  where the transmit message word signal  $M$  corresponds to a number representative of a message and

$$0 \leq M \leq n-1$$

$n$  being a composite number formed as a product of at least 3 ~~whole number factors greater than one,~~ the at least 3 factors being distinct random prime numbers, and

where the ciphertext word signal C corresponds to a number representative of an encoded form of said message through a relationship of the form

$$C \equiv a_e M^e + a_{e-1} M^{e-1} + \dots + a_0 \pmod{n}$$

where e and  $a_e, a_{e-1}, \dots, a_0$  are numbers; and

means for transmitting the ciphertext word signal C to the second station, wherein the second station includes means for deciphering the ciphertext word signal C using the at least 3 factors to produce the message.

New Claims:

14. (New Amended) A method of ~~processing~~communicating a message for use in ~~cryptographic communications~~cryptographically processed with an RSA public key encryption, comprising the steps of:

selecting a public key portion  $e$  associated with a recipient intended for receiving the message;

developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots, p_k-1$ , is relatively prime to the public key portion  $e$ ;

computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers; ~~and;~~

receiving a ciphertext message formed by encoding a plaintext message data  $M$  to a ciphertext message data  $C$  using a relationship of the form  $C \equiv M^e \pmod{n}$ , where  $M$  represents the message, where  $0 \leq M \leq n-1$  and where the sender knows  $n$  and the public key portion  $e$  but has no access to the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ ; and

deciphering at the recipient the received ciphertext message data  $C$  to produce the message, the recipient having access to the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ .

15. (NewAmended) The method according to claim 14, comprising the further step of:  
establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the form of

$$d \equiv e^{-1}(\text{mod}((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1))),$$

wherein the deciphering step includes decoding the ciphertext message data  $C$  to the plaintext message data  $M$  using a relationship of the form  $M \equiv C^d (\text{mod } n)$ .

16. (NewAmended) A method of ~~processing~~communicating a message ~~for use in cryptographic communications~~cryptographically processed with RSA public key encryption, comprising the steps of:

selecting a public key portion  $e$ ;

developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and checking that each of the  $k$  distinct random prime numbers minus 1,  $p_1 - 1, p_2 - 1, \dots, p_k - 1$ , is relatively prime to the public key portion  $e$ ;

establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the form of

$$d \equiv e^{-1}(\text{mod}((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1)));$$

computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers;

~~obtaining~~receiving a ciphertext message data  $C$ ; ~~and decoding the ciphertext message data  $C$  to~~  
representing an encoded form of a plaintext message data  $M$ ; and

decoding the received ciphertext message data  $C$  to the plaintext message data  $M$  using a  
relationship of the form  $M \equiv C^d (\text{mod } n)$ ; the decoding performed by a recipient owning  
the private key portion  $d$  and having access to the  $k$  distinct random prime numbers,  $p_1,$   
 $p_2, \dots, p_k$ .

17. (NewAmended) The method according to claim 16, ~~comprising the further step of:~~  
wherein the ciphertext message data  $C$  is formed by encoding the plaintext message data  $M$  to the  
ciphertext message data  $C$ ; using a relationship of the form  $C \equiv M^e \pmod{n}$ , wherein  $0 \leq M$   
 $\leq n-1$  and wherein  $n$  and the public key portion  $e$  are accessible to the sender although it has no  
access to the  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ .

18. (NewAmended) A method of ~~processing~~communicating a message ~~for use in~~  
~~cryptographic communications~~cryptographically processed with RSA public key encryption;  
comprising the steps of:

selecting a public key portion  $e$ ;

developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and checking that each  
of the  $k$  distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots, p_k-1$ , is relatively prime  
to the public key portion  $e$ ;

establishing a private key portion  $d$  by a relationship to the public key portion  $e$  of the form

$$d \equiv e^{-1} \pmod{((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1))};$$

computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers;

encoding a plaintext message data  $M$  with the private key portion  $d$  to produce a signed message  
 $M_s$  using a relationship of the form  $M_s \equiv M^d \pmod{n}$ , where  $0 \leq M \leq n-1$

receiving the signed message  $M_s$ ; and

deciphering the signed message to produce the plaintext message data  $M$ .

19. (NewAmended) The method of claim ~~18~~ further comprising ~~18,~~ wherein the deciphering  
step ofincludes:

decoding the signed message  $M_s$  with the public key portion  $e$  to produce the plaintext message  
data  $M$  using a relationship of the form  $M \equiv M_s^e \pmod{n}$ .

20. (New Amended) A method for ~~increasing the efficiency of communicating a cryptographic~~  
~~process~~message cryptographically processed with RSA public key encryption, comprising the  
steps of:

~~selecting a public key portion  $e$ ;~~

~~developing  $k$~~

sending to a recipient a cryptographically processed message formed by

assigning a number  $M$  to represent the message in plaintext message form, and

cryptographically transforming the assigned number  $M$  from the plaintext message form

to a number  $C$  that represents the message in an encoded form, wherein the  
number  $C$  is a function of

the assigned number  $M$ ,

a number  $n$  that is a composite number equaling the product of at least three

distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and checking

that each of the  $k$  wherein  $0 \leq M \leq n-1$ , and

an exponent  $e$  that is a number relatively prime to a lowest common multiplier of

the at least three distinct random prime numbers minus 1,  $p_1-1, p_2-1, \dots$

$p_k-1$ , is relatively prime to the public key portion  $e$ ;

computing a composite number,  $n$ , as a product of the  $k$  distinct random prime numbers; and,

wherein the number  $n$  and exponent  $e$  having been obtained by the sender are associated

with the recipient to which the message is intended; and

receiving the cryptographically processed message which is decipherable by the recipient based

on

the number  $n$ ,

another exponent  $d$ , and

the number  $C$ ,

wherein the exponent  $d$  is a function of the exponent  $e$  and the at least three distinct

random prime numbers.



21. (Amended) The method according to claim 20,

~~encoding a plaintext message data  $M$  to a ciphertext message data  $C$ , wherein the~~  
cryptographically transforming step includes using a relationship of the form  $C \equiv M^e$   
 $(\text{mod } n)$ , where  $0 \leq M \leq n-1$ ,

~~whereby a computational speed of the cryptographic process is increased.~~

~~21. (New) — The method according to claim 20, comprising the further step of:~~

~~establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the form of~~  
~~;~~~~and~~

~~decoding the ciphertext message data  $C$  to the plaintext message data  $M$  wherein the exponent  $d$~~   
is established based on the at least three distinct random prime numbers,  $p_1, p_2, \dots, p_k$ ,  
using a relationship of the form  $d \equiv e^{-1} (\text{mod}((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1)))$ , and

wherein the cryptographically processed message is deciphered using a relationship of the form  
 $M \equiv C^d (\text{mod } n)$ .

~~22. (New) Amended) A method for increasing the efficiency of communicating a cryptographic~~  
~~process message cryptographically processed with RSA public key encryption, comprising the~~  
~~steps of:~~

~~selecting a public key portion  $e$ ;~~

~~developing  $k$  distinct random prime numbers,  $p_1, p_2, \dots, p_k$ , where  $k \geq 3$ , and checking that each~~  
~~of~~

receiving from a sender a cryptographically processed message, in the form of a number  $C$ ,  
which is decipherable by the  $k$  distinct random prime numbers minus 1,  $p_1 - 1, p_2 - 1, \dots, p_k -$   
1, is relatively prime to the public key portion  $e$ ;

~~establishing a private key portion  $d$  by a relationship to the public key portion  $e$  in the form of~~  
~~;~~

~~computing recipient based on a composite number~~ number  $n$ ,  $n$ , as a product of the  $k$  distinct random prime numbers;

~~obtaining a ciphertext message data  $C$ ; and an exponent  $d$ , and the number  $C$ ; and~~

~~decoding the ciphertext~~ deciphering the cryptographically processed message data  $C$  to a,

wherein a number  $M$  represents a plaintext form of the message data  $M$ , wherein the number  $C$  represents a cryptographically encoded form of the message and is a function of

the number  $M$ ,

the number  $n$  that is a composite number equaling the product of at least three distinct random prime numbers, wherein  $0 \leq M \leq n-1$ , and

an exponent  $e$  that is a number relatively prime to a lowest common multiplier of the at least three distinct random prime numbers,

wherein the number  $n$  and exponent  $e$  are associated with the recipient to which the message is intended, and

wherein the exponent  $d$  is a function of the exponent  $e$  and the at least three distinct random prime numbers,

23. (Amended) The method according to claim 22,

wherein the number  $C$  is formed using a relationship of the form  $C \equiv M^e \pmod{n}$ ,

wherein the exponent  $d$  is established based on the at least three distinct random prime numbers,

$p_1, p_2, \dots, p_k$  using a relationship of the form  $d \equiv e^{-1} \pmod{((p_1 - 1) \cdot (p_2 - 1) \cdots (p_k - 1))}$ ,

and wherein the number  $M$  is obtained using a relationship of the form  $M \equiv C^d \pmod{n}$ ,

whereby a computational speed of the cryptographic process is increased.

23. (New) — The method according to claim 22, comprising the further step of:

encoding the plaintext message data  $M$  to the ciphertext message data  $C$ , using a relationship of

the form  $C \equiv M^e \pmod{n}$ , where  $0 \leq M \leq n-1$ .

<b>CONSENT OF ASSIGNEE TO REISSUE APPLICATION</b>		Docket Number: 20206-014(PT-TA-410)	
This is part of the application for a reissue patent based on the original patent identified below.			
Name of Patentee(s):	COLLINS et al.		
Patent Number:	5,848,159	Patent Issued	December 8, 1998
Title of Invention	PUBLIC KEY CRYPTOGRAPHIC APPARATUS AND METHOD		
<p>As an authorized agent empowered to act on behalf of <u>Compaq Computer Corporation</u>, the assignee of the entire interest in the original patent, I hereby consent to the filing of the present application for reissue of the original patent.</p> <p><input checked="" type="checkbox"/> A certificate under 37 CFR(b) is attached.</p>			
<p>I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under 18 U.S.C. 1001 and that such willful false statements may jeopardize the validity of the application, any patent issued thereon, or any patent to which this declaration is directed.</p>			
Name of Assignee	Compaq Computer Corporation		
Signature of Person Signing for Assignee			
Printed name and title of person signing for assignee	Theodore S. Park, Counsel		

IN THE UNITED STATES PATENTS AND TRADEMARK OFFICE

Applicant: COLLINS et al.

Attorney Docket No.: 20206-0014(PT-TA-410)

Patent No.: 5,848,159

Issued: December 8, 1998

For: "PUBLIC KEY CRYPTOGRAPHIC APPARATUS AND METHOD"

CERTIFICATE UNDER 37 CFR 3.73(b)

I. Compaq Computer Corporation, a Delaware corporation, certifies that it is the assignee of the entire right, title, and interest in the patent application identified above by virtue of a chain of title from the inventors of the patent application identified above, to the current assignee as shown below:

1. From: Thomas Collins, Dale Hopkins, Susan Langford and Michael Sabin  
To: Tandem Computers Incorporated

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2. From: Tandem Computers Incorporated  
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The document was recorded in the Patent and Trademark Office on October 12, 2000, a copy of which is attached.

II. The undersigned is empowered to sign this certificate on behalf of the assignee.

Date: 17 OCT 00



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5577-0404006  
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BRIEF: ASSIGNMENT OF ASSIGNOR'S INTEREST (SEE DOCUMENT FOR DETAILS).

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BRIEF: ARTICLES OF MERGER OF PATENT AND SUBSIDIARY CORPORATIONS

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**UNITED STATES PATENT AND TRADEMARK OFFICE**

Applicant(s): Collins et al.

Patent No. 5,848,159

Issued: December 8, 1998

By: LSB/jmp

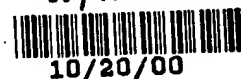
Docket No. 20206-014(PT-TA-410) Express No. EL655031318US

For: **PUBLIC KEY CRYPTOGRAPHIC APPARATUS AND METHOD**

The stamp of the U.S. Patent and Trademark Office hereon acknowledges receipt of the following:

1. Reissue Transmittal along with Fee Transmittal;
2. Petition to Wave Delay Period (37 CFR 1.183);
3. Specification and Claims for U.S. Patent No. 5,484,159;
4. Reissue Declaration by Inventors;
5. Offer to Surrender;
6. Certificate under 37 CFR 3.73(b);
7. Consent of Assignee to Reissue Patent;
8. Copy of Assignments;
9. Preliminary Amendment;
10. IDS Transmittal, 1449, and 13 cited references; and
11. Check No. 124516 for \$2,664.00.

JC914 U.S. PTO  
09/694416



Form 1449 (Modified)	Docket No. 20206.126	Reexamination No.: 90/005,773 90/009,333
Information Disclosure Statement By Applicant	Applicant:	
(Use Several Sheets if Necessary)	Filing Date 12-8-98	Group

### U.S. Patent Documents

Examiner Initial	No.	Patent No.	Date	Patentee	Class	Sub- class	Filing Date
JWS	A	4,351,982	9-28-82	Miller et al.	178	22.10; 22.11	12-15-80
JWS	B	5,974,151	10-26-99	Slavin	380	30	11-1-96
	C						
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	L						Yes	No
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### Other Documents

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Examiner <i>James Seal</i>	Date Considered <i>14 June 2002</i>
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Examiner: Initial citation considered. Draw line through citation if not in conformance and not considered. Include copy of this form with next communication to applicant.



FORM PTO-1449  U.S. DEPARTMENT OF COMMERCE, PATENT AND TRADEMARK OFFICE  INFORMATION DISCLOSURE STATEMENT BY APPLICANT	REISSUE APPLICATION NO. 09/694,416  REEXAMINATION CONTROL NO. 90/005/733  REEXAMINATION CONTROL NO. 90/005/733  Orig. PATENT NO. 5,848,159	ATTY DOCKET NO.:  20206-125 (PT-TA410) 20206-126 (PT-TA410US-4) 20206-127 (PT-TA410US-5) respectively.
	INVENTORS  COLLINS et al.	
	ISSUE DATE December 8, 1998	GROUP

## U. S. PATENT DOCUMENTS

EXAMINER INITIAL		DOCUMENT NUMBER	DATE	NAME	CLASS	SUBCLASS	FILING DATE IF APPROPRIATE
JWS	AA	4,514,592	4/30/1985	Miyaguchi	178	22.11; 22.14	7/14/1982
JWS	AB	5,046,094	9/3/1991	Kawamura	380	46; 28	2/2/1990
JWS	AC	5,343,527	8/30/1994	Moore	380	4; 25; 30	10/27/1993

## FOREIGN PATENT DOCUMENTS

		DOCUMENT NUMBER	DATE	COUNTRY	NAME	CLASS	SUBCLASS	TRANSLAT YES
	AD							

## OTHER DOCUMENTS (Including Author, Title, Date, Pertinent Pages, Etc.)

JWS	AE	P. J. Flinn et al. Using the RSA Algorithm for Encryption and Digital Signatures: Can you Encrypt, Decrypt, Sign and Verify without Infringing the RSA Patent?" July 9, 1997, Alston & Bird LLP, <a href="http://www.cyberlaw.com/rsa.html">http://www.cyberlaw.com/rsa.html</a>
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EXAMINER <i>James Seal</i>	DATE CONSIDERED 5 Dec 2001
EXAMINER: Initial if citation considered, whether or not citation is in conformance with MPEP 609; draw line through citation if not in conformance and not considered. Include copy of this form with next communication to applicant.	

FORM PTO-1449 U.S. DEPARTMENT OF COMMERCE PATENT AND TRADEMARK OFFICE  INFORMATION DISCLOSURE STATEMENT BY APPLICANT	ATTY DOCKET NO. 20206-0014(PT-TA-410)	PATENT NO. 5,848,159
	APPLICANT COLLINS et al.	
	ISSUE DATE December 8, 1998	GROUP 2766

## U. S. PATENT DOCUMENTS

EXAMINER INITIAL		DOCUMENT NUMBER	DATE	NAME	CLASS	SUBCLASS	FILING DATE IF APPROPRIATE
	AA	5,761,310	06/1998	Naciri	380	30	07/18/1996

## FOREIGN PATENT DOCUMENTS

		DOCUMENT NUMBER	DATE	COUNTRY	NAME	CLASS	SUBCLASS
	AB						

## OTHER DOCUMENTS (Including Author, Title, Date, Pertinent Pages, Etc.)

JWS	AC	S.A. VANSTONE et al., "Using Four-Prime RSA in Which Some of the Bits are Specified," December 1994, Electronics Letter, Vol. 30, No. 25. pp. 2118-2119.
JWS	AD	C. Couvruet et al., "An Introduction to Fast Generation of Large Prime Numbers," 1982, Philips Journal Research, Vol. 37, Nos. 5-6, pp. 231-264.
JWS	AE	Y. DESMEDT et al., "Public-Key Systems Based on the Difficulty of Tampering (Is There a Difference Between DES and RSA?)," 1986, Lecture Notes in Computer Science, Advances in Cryptology-CRYPTO '86. Proceedings.
JWS	AF	J. J. QUISQUATER et al., "Fast Decipherment Algorithm for RSA Public-Key Cryptosystem" October 1982, Electronic Letters, Vol. 19, No. 21.
JWS	AG	CETIN KAYA KOC, "High-Speed RSA Implementation (Version 2.0)," November 1994, RSA White Paper, RSA Laboratories.
JWS	AH	RIVEST et al., "A Method for Obtaining Digital Signatures and Public-Key Cryptosystems," February 1978, Communications of the ACM, Vol. 21.
JWS	AI	PKCS #1: RSA Encryption Standard (Version 1.5), November 1993, RSA Laboratories Technical Note.
JWS	AJ	M.O. RABIN, "Digitalized Signatures and Public-Key Functions as Intractable as Factorization," January, 1979, MIT Laboratory for Computer Science.
JWS	AK	R. LIDL et al., "Permutation Polynomials in RSA-Cryptosystems," 1984, Advances in Cryptology—Crypto '83, pp. 293-301.
JWS	AL	D. BONEH et al., "Generating a Product of Three Primes with an Unknown Factorization," Computer Science Department, Stanford University.
JWS	AM	J. J. QUISQUATER et al., "Fast Generation of Large Prime Numbers" June 1982, Library of Congress, Catalog No. 72-179437, IEEE Catalog No. 82CH1767-3 IT, pp. 114-115
JWS	AN	A. J. Menezes et al., "Handbook of Applied Cryptography", 1997, Library of Congress catalog No. 96-27609, pp. 89, 612-613

